| Surname |
| :--- |
| Other Names |


| Centre <br> Number |
| :---: |
|  |


| Candidate <br> Number |
| :--- |
| 0 |

## шјес cbac

## GCSE - NEW

## 3300U60-1

## MATHEMATICS

UNIT 2: CALCULATOR-ALLOWED
HIGHER TIER

## THURSDAY, 10 NOVEMBER 2016 - MORNING

## 1 hour 45 minutes

## Suitable for Modified Language Candidates

## ADDITIONAL MATERIALS

A calculator will be required for this paper.
A ruler, a protractor and a pair of compasses may be required.

## INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.
You may use a pencil for graphs and diagrams only.
Write your name, centre number and candidate number in the spaces at the top of this page.
Answer all the questions in the spaces provided.
If you run out of space, use the continuation page(s) at the back of the booklet, taking care to number the question(s) correctly.
Take $\pi$ as 3.14 or use the $\pi$ button on your calculator.

## INFORMATION FOR CANDIDATES

You should give details of your method of solution when appropriate.
Unless stated, diagrams are not drawn to scale.
Scale drawing solutions will not be acceptable where you are asked to calculate.
The number of marks is given in brackets at the end of each question or part-question.
In question 8, the assessment will take into account the quality of your linguistic and mathematical organisation, communication and accuracy in writing.

| For Examiner's use only |  |  |
| :---: | :---: | :---: |
| Question | Maximum Mark | Mark Awarded |
| 1. | 4 |  |
| 2. | 2 |  |
| 3. | 3 |  |
| 4. | 4 |  |
| 5. | 6 |  |
| 6. | 5 |  |
| 7. | 4 |  |
| 8. | 7 |  |
| 9. | 7 |  |
| 10. | 3 |  |
| 11. | 2 |  |
| 12. | 5 |  |
| 13. | 4 |  |
| 14. | 5 |  |
| 15. | 2 |  |
| 16. | 6 |  |
| 17. | 3 |  |
| 18. | 8 |  |
| Total | 80 |  |

## Formula List - Higher Tier

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=$ area of cross-section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


In any triangle $A B C$
Sine rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$
Area of triangle $=\frac{1}{2} a b \sin C$


## The Quadratic Equation

The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$ are given by $\quad x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

## Annual Equivalent Rate (AER)

AER, as a decimal, is calculated using the formula $\left(1+\frac{i}{n}\right)^{n}-1$, where $i$ is the nominal interest rate per annum as a decimal and $n$ is the number of compounding periods per annum.

1. (a) Reflect the triangle S in the line $y=x$.

(b) (i) Translate the triangle $S$ using the column vector $\binom{-5}{-4}$.

(ii) Write down the column vector that will reverse the translation in part (i).
2. The $n$th term of a sequence is given by $n^{2}+7$.

Write down the first three terms of this sequence.

$\qquad$
$\qquad$
$2^{\text {nd }}$ term $=$ $\qquad$

$$
3^{\text {rd }} \text { term }=
$$

年
$\qquad$
3. Circle the correct answer for each of the following.
(a) $x^{3} \times x^{6}=$

$$
\begin{array}{lllll}
x^{36} & x^{0.5} & x^{2} & x^{9} & x^{18}
\end{array}
$$

(b) $(7 x-5 y)-(3 x+2 y)=$
$4 x-3 y$
$4 x-7 y$
$4 x+3 y$
$-4 x+7 y$
$-4 x-7 y$
(c) A car travels $x$ miles in 30 minutes.

Its average speed in miles per hour is
$\frac{x}{2}$
$\frac{x}{30}$
$2 x$
$\frac{2}{x}$
$30 x$
4. A solution to the equation

$$
2 x^{3}-3 x-17=0
$$

lies between 2 and 3 .
Use the method of trial and improvement to find this solution correct to 1 decimal place. You must show all your working.
5. At a college, a total of 28 students study one or more of the science subjects: Biology, Chemistry and Physics.
The 28 students form the universal set, $\varepsilon$.
Some parts of the Venn diagram below have already been completed.
It is also known that:

- 13 students study Chemistry
(a) Complete the Venn diagram.


$$
\text { - } 5 \text { students study only Biology }
$$

$\varepsilon$
(b) How many students study Biology and Chemistry but not Physics?
...................................................................................................................................................................................
(c) One of the students is chosen at random.

What is the probability that this student studies Biology?
6. (a) The diagram below shows the graph of a straight line for values of $x$ from -3 to 3 .

(i) Write down the gradient of the above line.
(ii) Write down the equation of the line in the form $y=m x+c$, where $m$ and $c$ are whole numbers.
(b) Without drawing, show that the line $2 y=5 x-3$ is parallel to the line $4 y=10 x+7$. You must show working to support your answer.
7. A factory uses a machine to produce electrical sockets.

The manager carries out a survey to investigate the probability of the machine producing a socket that does not work (defective).

The relative frequency of defective sockets produced was calculated after testing a total of 1000 , 2000, 3000, 4000 and 5000 sockets.
The results are plotted on the graph below.

(a) How many of the first 3000 sockets tested were defective?
(b) Write down the best estimate for the probability that one socket, selected at random, will be defective.
You must give a reason for your choice.
Probability: $\qquad$
Reason: $\qquad$
8. In this question, you will be assessed on the quality of your organisation, communication and accuracy in writing.

Points $A, B, C$ and $D$ lie on the circumference of a circle, centre $O$.
$B D$ is a diameter of the circle.
The straight line $B C=4.7 \mathrm{~cm}$ and $B \widehat{A C}=28^{\circ}$.


Write down the size of $B \widehat{D C}$.
Hence, calculate the length $B D$.
You must show all your working.
9. (a) Factorise $x^{2}-2 x-24$, and hence solve $x^{2}-2 x-24=0$.
(b) Solve the equation $\frac{4 x-3}{2}+\frac{7 x+1}{6}=\frac{29}{2}$.
$\qquad$
10. Draw the enlargement of the given triangle, using

- a scale factor of -2 ,

Examiner


11. A rectangle measures 38 cm by 26 cm .

Each measurement is correct to the nearest cm.
Calculate the least possible area of the rectangle.
12. (a) Factorise $(x-7)^{2}+2(x-7)$.
(b) Factorise $12 x^{2}-27 y^{2}$.
$\qquad$
13. Make $x$ the subject of the following formula.

$$
a(x-b)=x(c-d)
$$

14. Points $E$ and $F$ lie on a circle, centre $O$. The radius of the circle is 10 cm . The area of the shaded sector is $65 \mathrm{~cm}^{2}$.


Diagram not drawn to scale
(a) Calculate the size of $E \hat{O} F$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) Hence, calculate the length of the arc $E F$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
15. Circle either TRUE or FALSE for each statement given below.

| GRAPH | STATEMENT |  |  |
| :---: | :---: | :---: | :---: |
|  | The equation of this graph could be $y=-x^{3}-2$. | TRUE | FALSE |
|  | The equation of this graph could be $y=x^{3}-9 x$. | TRUE | FALSE |
|  | The equation of this graph could be $y=x^{-1}$. | TRUE | FALSE |
|  | The equation of this graph could be $y=x^{3}+4$. | TRUE | FALSE |

$\qquad$
16. Use the quadratic formula to solve $(3 x-1)^{2}=x(2 x+3)+7$. Give your answers correct to 2 decimal places.
$\qquad$
17. Two similar shapes have areas of $700 \mathrm{~cm}^{2}$ and $140 \mathrm{~cm}^{2}$. The perimeter of the smaller shape is 83 cm .
Calculate the perimeter of the larger shape.
18. A 9-pointed star, with centre $O$, is shown below.

Each side of the star is of length $x \mathrm{~cm}$.
The distance from the centre to every inner vertex of the star is 7 cm . The distance from the centre to every outer vertex of the star is 10 cm .

(a) Calculate the perimeter of the star.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## (b) Calculate the area of the star.

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